# An Efficient Multi-Attribute Pattern Matching Machine 

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#### Abstract

We describe an efficient multi-attribute pattern matching machine to locate all occurrences of any of a finite number of the sequence of rule structures (called matching rules) in a sequence of input structures. The proposed algorithm enables us to match set representations containing multiple attributes. Therefore, in proposed algorithm, confirming transition is decided by the relationship, whether the input structure includes the rule structure or not. It consists in constructing a finite state pattern matching machine from matching rules and then using the pattern matching machine to process the sequence of input structures in a single pass. Finally, the pattern matching algorithm is evaluated by theoretical analysis and the evaluation is supported by the simulation results with rules for the extraction of keywords.


Key words: string pattern matching, set representation, multi-attribute pattern matching, finite state pattern matching machine, matching algorithm

## 1 Introduction

String pattern matching [Aho75, Aho90, Knut77, Aoe84, Fan93, Boye77] is an important component of many areas in science and information processing. A string pattern matching machine has been applied to various fields such as the lexical analysis of a compiler [Aho86], voice recognition [Take93], bibliographic search [Aho75], spelling checking [Pete80], text editing and so on. Aho and Corasick describe a simple, efficient string pattern matching machine [Aho75] (hereafter called C machine) to locate all occurrences of finite number of keywords in a text string in a single pass. However, in the AC machine, the input is restricted to characters. In addition, a multi-attribute input is very useful for many applications, such as, extraction of keywords [Kimo91, Ogaw93], document processing [Ikeh93], and so on. Moreover, the multi-attribute pattern matching is necessary for the realization of higher pattern matching.

This paper describes an efficient multi-attribute pattern matching machine (hereafter called MAPM machine) to locate all occurrences of any of a finite number of
matching rules in a sequence of input structures and a method for constructing the multi-attribute pattern matching machine. The proposed algorithm enables us to match set representations containing multiple attributes.

In the following chapters, the multi-attribute pattern matching scheme is described in detail. Chapter 2 explains an efficient string pattern matching machine based on Aho and Corasick. Chapter $\mathbf{3}$ describes the multi-attribute matching rules for the MAPM machine and an efficient algorithm for these matching rules. Chapter 4 explains the construction of the goto, output and failure functions for the MAPM machine. Chapter 5 shows the theoretical estimations and experimental evaluations for the MAPM machine. Finally, in Chapter 6 the future research is discussed.

## 2 The Aho-Corasick Algorithm

This chapter explains an efficient string pattern matching machine, where a finite state string pattern matching machine based on Aho and Corasick [Aho75] locates all occurrences of any of a finite number of keywords in a text string.

Let $K_{-} S E T$ be a finite set of strings which we shall call keywords and let $T X$ be an arbitrary string which we shall call the text string. The AC machine is a program which takes as input the text string $T X$ and produces as output the locations in $T X$ at which the keywords (elements of $K_{-} S E T$ ) appear as substrings. The AC machine is constructed as a set of states. Each state is represented by a number. The state number 0 represents an initial state.

With $I$ as the set of input symbols, the behavior of the AC machine is defined by next three functions:

```
goto function g:S\timesI->S\cup{fail},
failure function f:S->S,
output function output:S->A, subset of K_SET.
```

Figure 1 shows the functions, from Aho et. al., used by the machine AC for the set of keywords $K_{-} S E T=\{$ "another", "other", "to", "he", "with" $\}$. Here, $\neg\left\{{ }^{\prime}{ }^{\prime}{ }^{\prime},{ }^{\prime}{ }^{\circ} \mathrm{o}\right.$ ', 't', 'h', 'w'\} denotes all input symbols other than 'a', 'o', 't', 'h' or 'w'.

The directed graph in Figure 1 (a) represents the goto function. For example, the transition labeled ' $a$ ' from state 0 to state 1 indicates that $g\left(0,{ }^{\prime} a\right.$ ') $=1$. The absence of the arc indicates fail. The AC machine has the property that $g\left(0,{ }^{\circ} \sigma^{\prime}\right) \neq f$ fail for all input symbols $\sigma$. The behavior of the AC machine is summarized below.

(a) The goto function.

| $s$ | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 | 16 | 17 | 18 | 19 | 20 |
| :---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| $f(s)$ | 0 | 0 | 8 | 9 | 10 | 11 | 12 | 0 | 13 | 15 | 16 | 0 | 0 | 8 | 0 | 0 | 0 | 0 | 13 | 15 |

(b) The failure function.

| $s$ | output $(s)$ |
| :---: | :---: |
| 6 | $\{$ he $\}$ |
| 8 | $\{$ another, other $\}$ |
| 11 | $\{$ he $\}$ |
| 12 | $\{$ other $\}$ |
| 14 | $\{$ to $\}$ |
| 16 | $\{$ he $\}$ |
| 20 | $\{$ with $\}$ |

(c) The output function.

Figure 1: The function of the AC machine.

## Algorithm 1: The AC machine.

[Input]: A target text $T X=c_{1} c_{2} \ldots c_{n}$, where each $c_{i}$, for $1 \leq i \leq n$, is an input symbol and an AC machine with goto function $g$, failure function $f$, and output function output.
[Output]: Locations at which the keywords occur in $T X$.
[Method]:
begin
$s \leftarrow 0 ;$
for $i \leftarrow 1$ until $n$ do
begin
while $g\left(s, c_{i}\right)=$ fail do $s \leftarrow f(s)$;
$s \leftarrow g\left(s, c_{i}\right)$;
if output $(s) \neq \phi$ then
print $i$,output(s);
end
end
(Example 1) Consider the behavior of the AC machine that uses the functions in Figure 1 to process the text string "stothe". Since $g\left(0,{ }^{\prime} s^{\prime}\right)=0$, the machine enters the state 0 . Since $g\left(0,{ }^{\prime} \mathrm{t}^{\prime}\right)=13, g\left(13,{ }^{\prime} o^{\prime}\right)=14$, the AC machine enters state 14 ,
advances to the next input symbol and emits output(14), indicating that it has found the keywords "to" at the end of position 3 in the text string. In state 14 with the input symbol ' $t$ ', the AC machine makes two state transitions in its operating cycle. Since $g\left(14,{ }^{\prime} \mathrm{t}^{\prime}\right)=$ fail, the AC machine enters the state $8=f(14)$. At this point, since $g\left(8,{ }^{\prime} \mathrm{t}\right.$ ' $)=9$, the AC machine enters state 9 . Hereafter since $g\left(9,{ }^{\prime} \mathrm{h}\right.$ ') $=10, g\left(10,{ }^{\prime} \mathrm{e}^{\prime}\right)$ $=11$, the AC machine enters state 11 and computes the matching operation after detecting keyword "he". (END)

The AC algorithm consists in constructing a finite state pattern matching machine from the keywords and then using the machine to process the text string in a single pass. Construction of the AC machine takes a time proportional to the sum of the lengths of the keywords.

## 3 A Multi-Attribute Pattern Matching Algorithm

This chapter explains an algorithm of an efficient multi-attribute pattern matching machine (called MAPM machine). The MAPM machine is a extension of the AhoCorasick Algorithm. Section 3.1 describes the multi-attribute matching rules for the MAPM machine. In Section 3.2, an efficient algorithm of these matching rules is presented.

### 3.1 Matching rules for the MAPM machine

Let $A T T R$ be the attribute name and let VALUE be the attribute value. Let $R$ be a finite set of pairs ( $A T T R, V A L U E$ ), then we shall call $R$ a rule structure. For example, the following attributes are considered.
$S T R$ : string, that is, word spelling.
$C A T$ : category, or, a part of speech.
SEM : semantic information such as concepts and categories.
For example, the rule structure $R$ of "doctor" is defined using the above attributes as follows:

$$
R=\{(\text { ST R }, \text { "doctor" }),(\text { CAT }, \text { Noun }),(\text { SEM }, \text { Human })\}
$$

If $R U L E$ is the matching rule consisting of a sequence of rule structures, RULE is defined as follows:

$$
R U L E=R_{1} R_{2} \ldots R_{n}(1 \leq n)
$$

Let $R_{-} S E T$ be a set of $R U L E$.
(Example 2) Consider the following example of a $R_{-} S E T$.

$$
\begin{aligned}
& R_{-S} S E T=\left\{R U L E_{1}, R U L E_{2}\right\} \\
& R U L E_{1}=R_{1} R_{3}, R U L E_{2}=R_{2} R_{3} \\
& R_{1}=\{(S T R, \text { "male" })\} \\
& R_{2}=\{(S T R, \text { "female" })\} \\
& R_{3}=\{(S E M 1, \text { Male }),(\text { SEM } 2, \text { Imago })\}
\end{aligned}
$$

$R U L E_{1}$ is a rule to detect tautology expressions and $R U L E_{2}$ is a rule to detect contradictory expressions. For example, $R U L E_{1}$ can detect the expression of "male man" or "male bull" and so on, $R U L E_{2}$ can detect the expression of "female ram" or "female stallion" and so on. By using the multiple attributes for pattern matching, it is easy to define an abstraction rule. (END)

Input structures to be matched by rule structures are also defined by the same set representation. $N$ is used as the notation for input structures to distinguish them from $R$. In order to consider the abstraction of the rule structure, matching of the rule structure $R$ and the input structure $N$ are decided by the relationship such that $N$ includes $R(N \supseteq R)$.

### 3.2 A Matching Algorithm

Let $\alpha$ be a sequence of the input structures. The MAPM machine is a program which takes as input $\alpha$ and produces as output the locations in a $\alpha$ at which every RULE in $R_{-S} S T$ appears as subsequences of structures. The MAPM machine consists of a set of states. Each state is represented by a number. One state (usually 0 ) is designated as the initial state. The MAPM machine processes a $\alpha$ by successively reading the input structure $N$ in a $\alpha$, making state transitions and occasionally emitting an output.

Let $S_{e}$ be a set of states and let $J$ be a set of the rule structure $R$, then the behavior of the MAPM machine is defined by next three functions:

```
goto function \(g_{e}: S_{e} \times J \rightarrow S_{e} \cup\{\) fail \(\}\),
failure function \(f_{e}: S_{e} \rightarrow S_{e}\),
output function output \({ }_{e}: S_{e} \rightarrow A_{e}\), subset of R_SET.
```

Figure 2 shows the functions used by the machine MAPM for a R_SET = $\left\{R U L E_{1}, R U L E_{2}, R U L E_{3}, R U L E_{4}\right\}$. Here $\neg$ indicates all input structures except $R_{1}$ and $R_{3}$.

As the AC machine, the goto function $g_{e}$ maps a pair consisting of a state and an input structure into a state or the message fail. The directed graph in Figure 2 (a) represents the goto function. The failure function $f_{e}$ maps a state into a state. The failure function is constructed whenever the goto function reports fail. Certain states are designated as output states which indicate that a $R U L E$ has been found. The output function formalizes this concept by associating $R_{-S} S E T$ (possible empty) with every state.

In the MAPM machine, a confirming transition is decided by the relationship, whether the input structure $N$ includes the rule structure $R$ or not. Therefore, in order to confirm a transition from certain state to next_state using the relationship, we define a function CHECK (state, $N$ ) as follows:

## [Function CHECK (state, $N$ )]

For each transition $g_{e}($ state,$R)=$ next_state in the goto graph, if some transition labeled $R$ which satisfies the relationship ( $N \supseteq R$ ) exists, then it returns all next_state, otherwise it returns fail.
(Example 3) Suppose that $g_{e}\left(s_{1}, R_{1}\right)=s_{2}$ and $g_{e}\left(s_{1}, R_{2}\right)=s_{3}$ are defined in the goto graph and $R_{1}$ and $R_{2}$ are defined as follows:

(a) The goto function.

(d) $R \_S E T=\{R U L E 1, R U L E 2, R U L E 3, R U L E 4\}$.

Figure 2: The functions of the MAPM machine for $R_{-} S E T$.

$$
\begin{aligned}
& R_{1}=(S E M, \text { Human }) \\
& \left.R_{2}=(C A T, \text { Noun })\right)
\end{aligned}
$$

Consider the behavior of the function CHECK to process the following $N_{1}$ and $N_{2}$.

$$
\begin{aligned}
& N_{1}=(S T R, \text { "mother") },(\text { CAT, Noun }),(\text { SEM, Human }) \\
& N_{2}=(S T R, \text { "beautiful" }),(C A T, \text { Adjective })
\end{aligned}
$$

For $N_{1}$ the function CHECK returns $s_{2}$ and $s_{3}$ to satisfy $R_{1} \subseteq N_{1}$ and $R_{2} \subseteq N_{1}$. In the case of $N_{2}, R_{1} \subseteq N_{2}$ and $R_{2} \subseteq N_{2}$ are not satisfied, therefore the function CHECK returns fail. (END)

Algorithm 2 summarizes the behavior of the MAPM machine.

Algorithm 2: A Multi-Attribute Pattern Matching machine (MAPM machine).
[Input]: A sequence of input structures $\alpha=N_{1}, N_{2}, \ldots, N_{n}$, where each $N_{i}$ is an input structure and a MAPM machine with goto function $g_{e}$, failure function $f_{e}$, and output function output ${ }_{e}$.
[Output]: Locations at which sequences of structure were extracted.
[Method]:
begin
queue ${ }_{1} \leftarrow 0$;
for $i \leftarrow 1$ until $n$ do
begin
$q u e u e_{2} \leftarrow$ empty;
while queue ${ }_{1} \neq \phi$ do
begin temp $\leftarrow$ empty; let state be the next state in queue ${ }_{1}$; queue $_{1} \leftarrow$ queue $_{1}$ - state; while $\operatorname{CHECK}\left(\right.$ state, $\left.N_{i}\right)=$ fail do state $\leftarrow f_{e}($ state $)$; temp $\leftarrow \operatorname{CHECK}\left(\right.$ state, $\left.N_{i}\right) ;$ $q u e u e_{2} \leftarrow$ queue $_{2} \cup$ temp; while temp $\neq \phi$ do

## begin

let element be the next state in temp;
tem $p \leftarrow$ temp - element;
if output ${ }_{e}($ element $) \neq \phi$ then begin
print $i$;
output $_{e}($ element $)$ end
end
end;
$q u e u e_{1} \leftarrow$ queue $_{2}$
end
end.

As we have mentioned before, in this algorithm, confirming transitions are decided by the relationship ( $N \supseteq R$ ). Therefore, it has the possibility that some $R$ such that $N$ includes $R$ exist among those transitions. In order to solve this problem, Algorithm 2 stores all states returned by the function CHECK in a first-in-first-out list denoted by the variable queue ${ }_{1}$, and the MAPM machine continues to process for each state in queue ${ }_{1}$.
(Example 4) Figure 2 shows the functions used by the MAPM machine for a $R_{-} S E T=$ $R U L E_{1}, R U L E_{2}, R U L E_{3}, R U L E_{4}$. Consider the behavior of the MAPM machine that uses the functions in Figure 2 to process the sequence of the input structures $\alpha=N_{1} N_{2} N_{3} N_{4} N_{5} N_{6}$.

$$
\begin{aligned}
& N_{1}=(S T R, \text { "beautiful" }),(\text { CAT, Adjective }) \\
& N_{2}=(S T R, \text { "rose" }),(\text { CAT, Noun }),(S E M 1, \text { Flower })
\end{aligned}
$$

```
\(N_{3}=(S T R, " a n d "),(C A T\), Conjunction \()\)
\(N_{4}=(S T R, " p r e t t y "),(C A T\), Adjective \()\)
\(N_{5}=(S T R, "\) girl"), (CAT, Noun \(),(\) SEM1, Human \(),(\) SEM2, Female \()\)
\(N_{6}=(S T R\), "are"), (CAT, Verb)
```

Since $N_{1}$ includes $R_{1}$ and $N_{2}$ includes $R_{2}, \operatorname{CHECK}\left(0, N_{1}\right)=1$ and $\operatorname{CHECK}\left(1, N_{2}\right)$ $=2$, the MAPM machine enters state 2, advances to the next input structure and emits the output $e_{e}(2)$, indicating that it has found the $R U L E_{1}$ at the end of position 2 in the $\alpha$. Since $N_{3}$ doesn't include $R_{1}$ or $R_{3}, \operatorname{CHECK}\left(0, N_{3}\right)=0$, the MAPM machine enters the state 0 . Since $N_{4}$ includes $R_{1}$ and $N_{5}$ includes $R_{3}$, $\operatorname{CHECK}(0$, $\left.N_{4}\right)=1, \operatorname{CHECK}\left(1, N_{5}\right)=3$, the MAPM machine enters state 3 . In state 3 with the input structure $N_{6}$, the MAPM machine makes two state transitions in this operating fashion. Since $N_{6}$ doesn't include $R_{4}, \operatorname{CHECK}\left(3, N_{6}\right)=$ fail, the MAPM machine enters the state $6=f_{\epsilon}(3)$. At this point, since $N_{6}$ includes $R_{6}, \operatorname{CHECK}\left(6, N_{6}\right)=7$, the MAPM machine enters state 7, emits output $(7)$, indicating that it has found the $R U L E_{3}$ at the end of position 6 in the $\alpha$. (END)

The MAPM algorithm consists in constructing a finite state pattern matching machine from matching rules and then using the machine to process the sequence of input structures in a single pass.

## 4 Construction of Goto, Output and Failure Function for the MAPM Machine

This chapter explains the construction of the goto, output and failure function for the MAPM machine. Although the construction of the MAPM machine is similar to the construction of the AC machine [Aho75], the point which changes a transition label for the goto function to a set is different from the AC machine. Therefore, the decision of the same transition when the goto, failure and output functions are constructed is defined as follows:

## [Condition for the equivalency of rule structures]

If the number of elements of rule structure $R_{1}$ and $R_{2}$ are equal and each of the elements (ATTR,VALUE) of $R_{1}$ and $R_{2}$ are equal, then we define $R_{1}$ equal to $R_{2}$ ( $R_{1}=R_{2}$ ).

In order to examine the equivalency of rule structures, we define a function $\operatorname{ARC}($ state,$R)$. The function ARC returns a next_state that satisfies the condition for the equivalency of rule structures. The following shows the function ARC.
[Function $\operatorname{ARC}\left(\right.$ state, $\left.R_{2}\right)$ ]
For each transition $g_{e}\left(\right.$ state,$\left.R_{1}\right)=$ next_state in the goto graph, if $R_{1}=R_{2}$, then the function ARC returns a next_state, otherwise it returns fail.
(Example 5) Suppose that $g_{e}\left(\right.$ state $\left._{1}, R_{1}\right)=$ state $_{2}$ is defined in the goto graph and $R_{1}$ is defined as:

$$
R_{1}=(C A T, \text { Noun }),(\text { SEMHuman })
$$

Consider the behavior of the function ARC to process the following rule structures $R_{2}$ and $R_{3}$ :

$$
\begin{aligned}
& R_{2}=(C A T, \text { Noun }),(\text { SEM }, \text { Human }) \\
& R_{3}=(C A T, \text { Noun })
\end{aligned}
$$

For $R_{2}$, ARC returns state s $_{2}$ to satisfy the condition for the equivalency of rule structures $R_{1}=R_{2}$. For $R_{3}$, the function CHECK doesn't satisfy the condition for the equivalency of rule structures $R_{1}=R_{3}$ and therefore returns fail. (END)

Algorithm 3 summarizes the method for the construction of the goto and output functions for the MAMP machine. Algorithm 4 summarizes the method for the construction of the failure and output functions for the MAMP machine.

Algorithm 3: Construction of the goto function.
[Input]: Set of RULE $R_{-} S E T=R U L E_{1}, R U L E_{2}, \ldots, R U L E_{k}$.
[Output]: Goto function $g_{e}$ and a partially computed output function outpute.
[Method]: We assume output $(s)$ is empty when state $s$ is first created, and $g_{e}(s, R)=$ fail if $R$ is undefined or if $g_{e}(s, R)$ has not yet been defined. The procedure enter $(R U L E)$ inserts into the goto graph a path that spells out RULE.

```
begin
    newstate \(\leftarrow 0\);
    for \(i \leftarrow 1\) until \(k\) do enter \(\left(R U L E_{i}\right)\);
    end
    procedure enter \(\left(R_{1}, R_{2}, \ldots, R_{m}\right)\)
    begin
        state \(\leftarrow 0 ; j \leftarrow 1\);
        while \(\mathrm{ARC}\left(\right.\) state,\(\left.R_{j}\right) \neq\) fail do
                begin
                state \(\leftarrow \mathrm{ARC}\left(\right.\) state, \(\left.R_{j}\right) ;\)
                \(j \leftarrow j+1\)
        end
    for \(p \leftarrow j\) until \(m\) do
        begin
            newstate \(\leftarrow\) newstate +1 ;
            \(g_{e}\left(\right.\) state,\(\left.R_{p}\right) \leftarrow\) newstate;
            state \(\leftarrow\) newstate;
            end
        output \(_{e}(\) state \() \leftarrow R_{1}, R_{2}, \ldots, R_{m}\)
    end
```

    for all \(R\) such that \(\operatorname{ARC}(0, R)=\) fail do \(g_{e}(0, R) \leftarrow 0\);
    Algorithm 4: Construction of the failure function.
[Input]: Goto function $g_{e}$ and output function output $t_{e}$ from Algorithm 3.
[Output]: Failure function $f_{e}$ and output function output $e_{e}$.
[Method]:
begin
queue $\leftarrow$ empty;
for each $R$ such that $\operatorname{ARC}(0, R)=s \neq 0$ do
begin
queue $\leftarrow$ queue $\cup s$;
$f_{e}(s) \leftarrow 0$
end
while queue $\neq$ empty do
begin
let $r$ be the next state in queue;
queue $\leftarrow q u e u e-r$;
for each $R$ such that $\operatorname{ARC}(r, R)=s \neq$ fail do
begin
queue $\leftarrow$ queue $\cup s$;
state $\leftarrow f_{e}(r)$;
while $\operatorname{ARC}($ state,$R)=$ fail do state $\leftarrow f_{e}($ state $)$;
$f_{e}(s) \leftarrow \operatorname{ARC}($ state,$R) ;$
output $_{e}(s) \leftarrow$ output $_{e}(s) \cup$ output $_{e}\left(f_{e}(s)\right)$
end
end
end
(Example 6) Consider the construction of the MAPM machine for the R_SET = $R U L E_{1}, R U L E_{2}, R U L E_{3}, R U L E_{4}$ in Figure 2 (d). In the first place, the states and the goto function are determined according to Algorithm 3. Second, the failure function is computed according to Algorithm 4. The output function is constructed according to both Algorithms. The decision of the same transition when the goto, failure and output functions are constructed is decided by the equivalency of the rule structures.

Firstly, consider the construction of goto function. Adding the first rule RULE to the graph, $g_{e}\left(0, R_{1}\right)=1$ and $g_{e}\left(1, R_{2}\right)=2$ are constructed as shown in Figure 3 (a). At this point, the output " $R_{1}, R_{2}$ " is associated with state 2 .

Adding the second rule $R U L E_{2}$, Figure $3(\mathrm{~b})$ is obtained. Since $\operatorname{ARC}\left(0, R_{1}\right)$ $=1$, notice that when the rule structure $R_{1}$ in $R U L E_{2}$ is added there is already a transition labeled " $R_{1}$ " from state 0 to state 1 . Therefore it is not needed to add another transition labeled " $R_{1}$ " from state 0 to state 1 . After that, $g_{e}\left(1, R_{3}\right)=3$, $g_{e}\left(3, R_{4}\right)=4$ and $g_{e}\left(4, R_{5}\right)=5$ are constructed as shown Figure 3 (b). The output " $R_{1}, R_{3}, R_{4}, R_{5}$ " is associated with state 5 .

Adding the third rule $R U L E_{3}, g_{e}\left(0, R_{3}\right)=6$ and $g_{e}\left(6, R_{6}\right)=7$ are constructed as shown in Figure 3 (c). The output " $R_{3}, R_{6}$ " is associated with state 7 .

Adding the last rule $R U L E_{4}$, Figure 3 (d) is obtained. The output " $R_{3}, R_{6}, R_{1}$ " is associated with state 8 . Here, since $\operatorname{ARC}\left(0, R_{3}\right)=6$ and $\operatorname{ARC}\left(6, R_{6}\right)=7$, we have been able to use the existing transition labeled $R_{3}$ from state 0 to state 6 and the

(a) The graph for RULE1.

(b) The graph for RULE 1 and RULE2.

(c) The graph for RULE1, RULE 2 and RULE3.

(d) The graph for RULE1, RULE2, RULE 3 and RULE4.

(e) The graph for R_SET.

Figure 3: The construction of the goto graph for $R_{-} S E T$.
existing transition labeled $R_{6}$ from state 6 to state 7 . To complete the construction of the goto function, a loop from state 0 to state 0 on all the input structures other than " $R_{1}$ " and " $R_{3}$ ", is added to the graph. Finally, Figure $3(e)$ is obtained.

Next, consider the construction of the failure function. To compute the failure function from Figure $3(\mathrm{e}), f_{e}(1)=f_{e}(6)=0$ is set since state 1 and 6 are the states of depth 1 . Then the failure function for state 2,3 and 7 , the states of depth 2 , is computed. To compute $f_{e}(2)$, state $=f_{e}(1)=0$ is set; and since $\operatorname{ARC}\left(0, R_{2}\right)=$ $0, f_{e}(2)=0$ is determined. To compute $f_{e}(3)$, state $=f_{e}(1)=0$ is set, and since $\operatorname{ARC}\left(0, R_{3}\right)=6, f_{e}(3)=6$ is determined. To compute $f_{e}(7)$, state $=f_{e}(6)=0$ is set; and since $\operatorname{ARC}\left(0, R_{6}\right)=0, f_{e}(7)=0$ is determined. Continuing in this fashion, the failure function shown in Figure 2 (b) is obtained.

Finally, the goto, failure and output functions are constructed as shown in Figure 2 (b) and (c). (END)

## 5 Evaluation

In this chapter, the theoretical estimations and experimental evaluations for the MAPM machine are presented. Section 5.1, describes the theoretical estimations for the MAPM machine, and in Section 5.2, it is evaluated by applying it to the extraction of keywords [Kimo91, Ogaw93].

### 5.1 Theoretical Estimations

Suppose that the time complexity for confirming a transition in the MAPM machine is $O(1)$. Let $m$ be the length of sequence of input structures $\alpha$. The time complexity of matching Algorithm 2 by the MAPM machine is $\mathrm{O}(m)$, because the matching cost of the AC machine is independent of the number of matching rules (keywords). However, the precise complexity for confirming a transition depends on the cost of the function CHECK and queue ${ }_{1}$ in Algorithm 2.

Consider the time complexity of the function CHECK. By using the order of attributes names, sets of input and rule structures can be represented as the sortedlist whose nodes are denoted by (attribute-name, attribute-value, pointer). Similarly, the goto function is represented by the list structure. Let $K$ be the kinds of attribute names. In the function CHECK, the time complexity for judging the relationship, whether the input structure includes the rule structure or not, is similar to the cost $(K+K=2 K)$ of merging two sorted_lists of maximum length $K$ into one list. Therefore, the time complexity of judging the relationship is $\mathrm{O}(K)$. Suppose that $B$ is the maximum number of transitions leaving from certain state $s$. Then, the time complexity of the function CHECK is $\mathrm{O}(K B)$. Although this cost is more than that of the AC machine, an expression ability of rules for the MAPM machine is higher than the rule for the AC machine.

From the above observation, consider the time complexity of confirming a transition. Let $D$ be the maximum number of the states in queue ${ }_{1}$. The complexity is $\mathrm{O}(K B D)$, because $q u e u e_{1}$ has all states returned by the function CHECK in Algorithm 2.

The time complexity for constructing the AC machine is proportional to the total length $h$ of keywords. On the other hand, the time complexity for the construction of the MAPM machine is $\mathrm{O}(h K)$ in the worst-case, because confirming transitions depends on the function ARC and the time complexity for determining the equivalency of the rule structures in the function ARC is the same cost $O(K)$ as the function CHECK.

### 5.2 Experimental Evaluations

The MAPM machine is evaluated by applying it to the extraction of keywords [Kimo91, Ogaw93]. For experimental evaluations, the MAPM machine has been implemented on a DELL OptiPlex GXMT5133 and it has been written in the C language.

In order to evaluate the efficiency of the proposed algorithm, we defined 112 rules for the extraction of keywords. Table 1 shows the information about the rules for the extraction of keywords. The information about RULE are the values for each

| Total number of kinds of attribute names | 5 |
| :--- | :---: |
| Information about RULE |  |
| $\quad$ Total number | 112 |
| $\quad$ Average length | 2.5 |
| $\quad$ Average number of kind of attributes names | 1.9 |
| Construction time of the MAPM machine [sec] | 0.543 |

Table 1: Information about $R U L E$ and construction time.

|  | Text1 | Text2 | Text3 | Average |
| :--- | :---: | :---: | :---: | :---: |
| Number of words | 411 | 233 | 197 | 280.0 |
| Matching time [ms] | 20.9 | 10.3 | 7.4 | 12.9 |
| Number of extracted keywords | 18 | 15 | 15 | 16.0 |

Table 2: The results of the simulation.
rule structure. From the average number, 1.9, of kinds of attribute names, it turns out that the attribute of each structure was abstracted effectively. It seems that the construction time (CPU time), 0.543 second, is practical.

Table 2 shows the results of the simulation using the above rule. To perform the simulation of the extraction of keywords, the following three texts were used.

Text1: General document, such as letter, journal, etc.
Text2: Abstract of a paper.
Text3: Document of patents.
From the average matching time in Table 2, the efficiency of the proposed algorithm could be verified. As shown by the theoretical estimations, the time complexity of the MAPM machine depends on the cost of the function CHECK. In the simulation, the attribute of each structure was abstracted effectively, such that the average of number of kinds of attribute names is 1.9. Consequently, good results could be obtained.

## 6 Conclusions

We have described an efficient method for multi-attribute pattern matching in this paper. A multi-attribute pattern matching is useful for many applications and the proposed algorithms enable the realization of higher pattern matching. The presented algorithm are evaluated by theoretical estimation and the experimental evaluation is supported by simulation results for the extraction of keywords.

In the proposed algorithms, it takes time to judge whether the input structure includes the rule structure or not. Therefore, as future extension, we are considering an efficient data structure and an efficient decision algorithm for the judging of the relationship, whether the input structure includes the rule structure or not. We
believe the proposed method is very useful for any existing and future computing system that would require an efficient multi-attribute pattern matching.

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