

Lexicalized Syntactic Analysis by Restarting Automata

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- 2 Definitions
- 3 Sensitivity of Lexicalized Constructions
- 4 Contextually Transparent Constructions
- 5 Conclusions

Lexicalized Syntactic Analysis

1 input sentence

PSC means an interesting conference

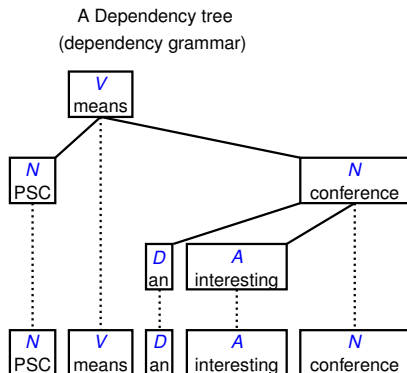
Lexicalized Syntactic Analysis

- 1 input sentence
- 2 lexicalization

<i>N</i> PSC	<i>V</i> means	<i>D</i> an	<i>A</i> interesting	<i>N</i> conference
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Lexicalized Syntactic Analysis

- 1 input sentence
- 2 lexicalization
- 3 lexicalized syntactic analysis
– “Does the tagged word forms constitute a grammatically correct sentence which is correctly tagged?”



Analysis by Reduction

The German team won the World Cup in Brazil.

Analysis by Reduction

*The **German** team won the World Cup in Brazil.*

The team won the World Cup in Brazil.

- ← each reduction
 - preserves (non)correctness
 - is local
 - shortens

Analysis by Reduction

The German team won the World Cup in Brazil.

*The team won the **World** Cup in Brazil.*

The team won the Cup in Brazil.

← each reduction

- preserves (non)correctness
- is local
- shortens

Analysis by Reduction

The German team won the World Cup in Brazil.

The team won the World Cup in Brazil.

*The team won **the Cup** in Brazil.*

The team won in Brazil.

← each reduction

- preserves (non)correctness
- is local
- shortens

Analysis by Reduction

The German team won the World Cup in Brazil.

The team won the World Cup in Brazil.

The team won the Cup in Brazil.

*The team won **in Brazil**.*

The team won.

← each reduction

- preserves (non)correctness
- is local
- shortens

Analysis by Reduction

The German team won the World Cup in Brazil.

The team won the World Cup in Brazil.

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- ← each reduction
 - preserves (non)correctness
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- ← simple correct sentence, hence Accept

Analysis by reduction

- checking correctness of sentences

Analysis by Reduction

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Analysis by reduction

- checking correctness of sentences
- localizing errors

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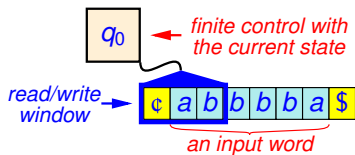
- ← each reduction
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- ← simple correct sentence, hence Accept

Analysis by reduction

- checking correctness of sentences
- localizing errors
- detecting (in)dependencies within a sentence

Restarting Automaton

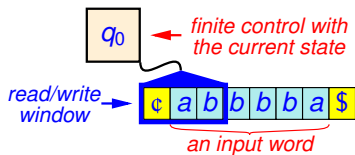
RLWW-automaton



- a finite set of states Q

Restarting Automaton

RLWW-automaton

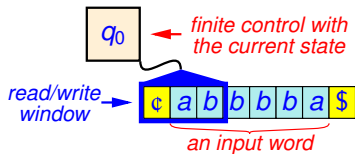


■ a finite set of states Q

■ an input alphabet Σ

Restarting Automaton

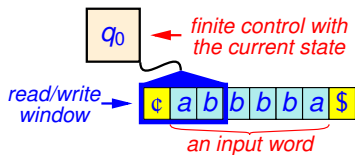
RLWW-automaton



- a finite set of states Q
- an input alphabet Σ
- a working alphabet $\Gamma (\supseteq \Sigma)$

Restarting Automaton

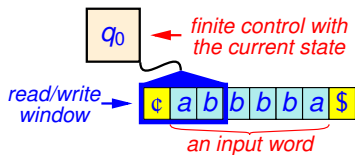
RLWW-automaton



- a finite set of *states* Q
- an *input alphabet* Σ
- a *working alphabet* $\Gamma (\supseteq \Sigma)$
- the left and right *sentinels* \mathfrak{c} and $\mathfrak{\$}$

Restarting Automaton

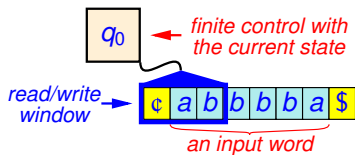
RLWW-automaton



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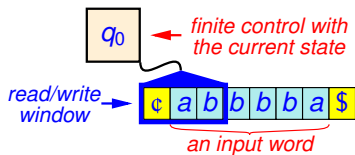
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- the left and right *sentinels* \mathfrak{c} and $\mathfrak{\$}$
- the *initial state* q_0
- a *read/write window* of length k

Restarting Automaton

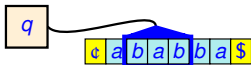
RLWW-automaton



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- an input alphabet Σ
- a working alphabet $\Gamma (\supseteq \Sigma)$
- the left and right sentinels \clubsuit and $\$$
- the initial state q_0
- a read/write window of length k
- a partial transition function δ

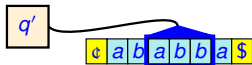
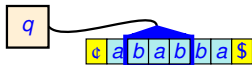
RLWW-Automaton

Possible Steps



RLWW-Automaton

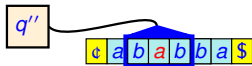
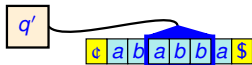
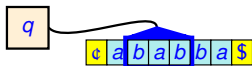
Possible Steps



- **move right** and change the state

RLWW-Automaton

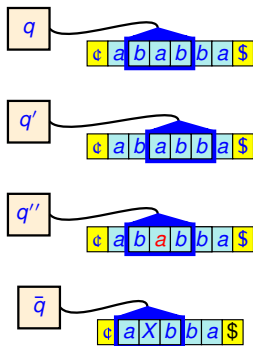
Possible Steps



- move right and change the state
- **move left** and change the state

RLWW-Automaton

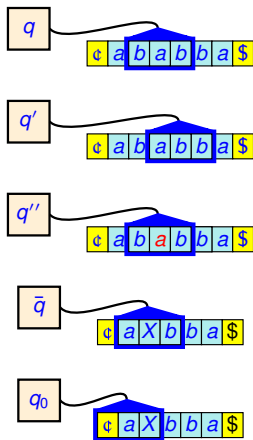
Possible Steps



- move right and change the state
- move left and change the state
- **rewrite**
 - **must shorten** the tape,
 - “complete” the window from the left
 - a new state is entered,

RLWW-Automaton

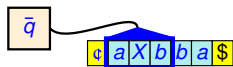
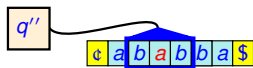
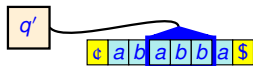
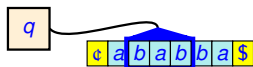
Possible Steps



- move right and change the state
- move left and change the state
- rewrite
 - must shorten the tape,
 - “complete” the window from the left
 - a new state is entered,
- **restart**

RLWW-Automaton

Possible Steps



- move right and change the state
- move left and change the state
- rewrite
 - must shorten the tape,
 - “complete” the window from the left
 - a new state is entered,
- restart
- **accept**

RLWW-Automaton

How It Computes

- general RLWW-automata are **nondeterministic**

RLWW-Automaton

How It Computes

- general RLWW-automata are nondeterministic
- if for a given state and contents of the read/write window the automaton has **no instruction**, then the automaton **halts and rejects**

RLWW-Automaton

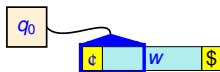
How It Computes

- general RLWW-automata are nondeterministic
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- **rewrite and restart steps must alternate**

RLWW-Automaton

How It Computes

- general RLWW-automata are nondeterministic
- if for a given state and contents of the read/write window the automaton has no instruction, then the automaton halts and rejects
- rewrite and restart steps must alternate
- a word $w \in \Sigma^*$ is **accepted** if there exists a computation starting in the initial state q_0 with w on the tape

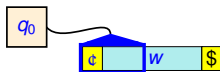


and ending with an *accept* step

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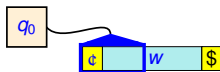
- the **input language** accepted by \mathcal{M}

$$L(\mathcal{M}) = \{w \in \Sigma^* \mid \mathcal{M} \text{ accepts } w\}$$

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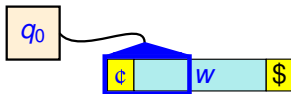
- the **basic language** accepted by \mathcal{M}

$$L_C(\mathcal{M}) = \{w \in \Gamma^* \mid M \text{ accepts } w\}$$

RLWW-Automaton

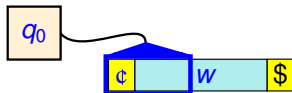
Cycles

- a restarting configuration:



RLWW-Automaton

Cycles



■ a **restarting configuration**:

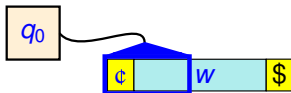
■ a **cycle** – each part of a computation:

$\langle \text{restarting configuration}_1 \rangle \rightsquigarrow \langle \text{restarting configuration}_2 \rangle$

notation: $w \Rightarrow_{\mathcal{M}}^c w'$ if there is a cycle from restarting configuration with w on the tape and ending by the restart with w' on the tape

RLWW-Automaton

Cycles



- a **restarting configuration**:

- a **cycle** – each part of a computation:

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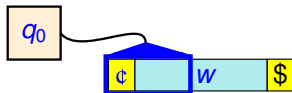
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- a **tail** – the last part of a computation:

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RLWW-Automaton

Cycles



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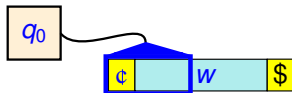
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- a **computation**: a sequence of cycles finished by a tail

RLWW-Automaton

Cycles



- a **restarting configuration**:
- a **cycle** – each part of a computation:
 - $\langle \text{restarting configuration}_1 \rangle \rightsquigarrow \langle \text{restarting configuration}_2 \rangle$
 - notation: $w \Rightarrow_{\mathcal{M}}^c w'$ if there is a cycle from restarting configuration with w on the tape and ending by the restart with w' on the tape
- a **tail** – the last part of a computation:
 - $\langle \text{restarting configuration} \rangle \rightsquigarrow \langle \text{halting configuration} \rangle$
- a **computation**: a sequence of cycles finished by a tail
- a **RLWW(i)-automaton**: can execute at most i rewrite instructions per cycle

h-Lexicalized RLWW(i)-automaton

hRLWW(i)-Automaton

$\hat{M} = (M, h)$ where

M is an RLWW(i)-automaton

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- the **input language** $L(\hat{M}) = L(M)$

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- the **basic language** $L_c(\hat{M}) = L_c(M)$

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- the **input language** $L(\hat{M}) = L(M)$
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- the **h-proper language** accepted by \hat{M}

$$L_{hP}(\hat{M}) = h(L_C(M))$$

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- **h-lexicalized syntactic analysis**

$$L_A(\widehat{M}) = \{(h(w), w) \mid w \in L_C(M)\}$$

h-Lexicalized RLWW(i)-automaton

hRLWW(i)-Automaton

$\hat{M} = (M, h)$ where

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- **h-lexicalized syntactic analysis**

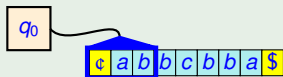
$$L_A(\hat{M}) = \{(h(w), w) \mid w \in L_C(M)\}$$

- obviously $L(\hat{M}) \subseteq L_{\text{hP}}(\hat{M}) = h(L_C(\hat{M}))$

RLWW-Automaton Accepting Palindromes with Marked Centers

$$L_{pal,c} = \{wcw^R \mid w \in \{a,b\}^*\}$$

Example 1

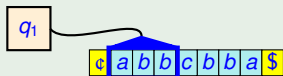


- (1) $\delta(q_0, cc\$) = \{\text{Accept}\},$
- (2) $\delta(q_0, cxy) = \{(q_1, \text{MVR})\},$
for all $x \in \{a, b\}, y \in \{a, b, c\},$
- (3) $\delta(q_1, aca) = \{(q_2, c)\},$
- (4) $\delta(q_1, bcb) = \{(q_2, c)\},$
- (5) $\delta(q_1, xyz) = \{(q_1, \text{MVR})\},$
for all $x, y \in \{a, b\}, z \in \{a, b, c\},$
- (6) $\delta(q_2, u) = \{\text{Restart}\},$
for all $u \in \Gamma^3 \cup \Gamma^{\leq 2} \cdot \{\$\}.$

RLWW-Automaton Accepting Palindromes with Marked Centers

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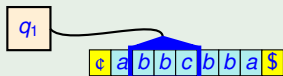


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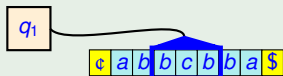


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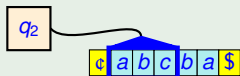


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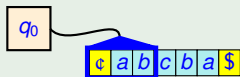


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RLWW-Automaton Accepting Palindromes with Marked Centers

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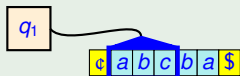


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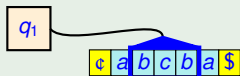


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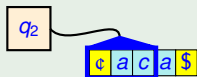


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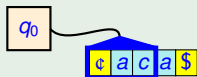


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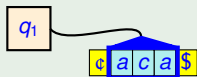


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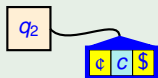


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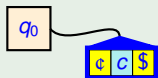


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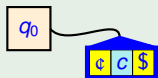
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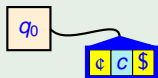
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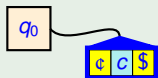
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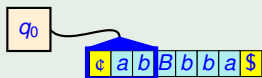
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RLWW-Automaton Accepting Even Palindromes

$$L_{pal} = \{ ww^R \mid w \in \{a, b\}^* \}$$

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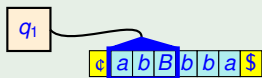


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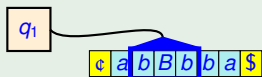


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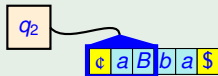


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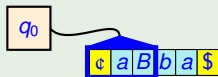


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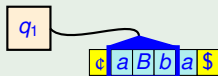


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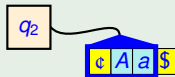


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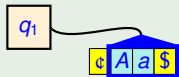


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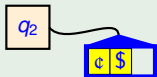


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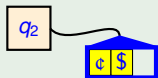
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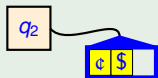
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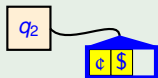
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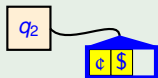
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The Power of RLWW(*i*)-automata

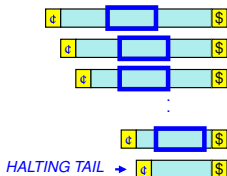
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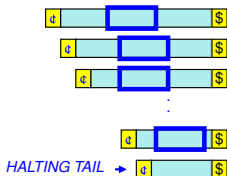
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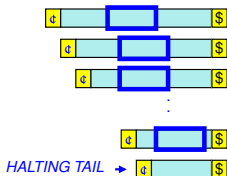


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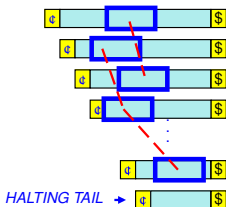


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- $\mathcal{L}(\text{mon-RLWW}(1)) = \text{CFL}$

j -Monotone Automata

- a j -monotone computation: the places of rewriting can be partitioned into at most j (noncontiguous) monotone subsequences



subsequences

- a j -monotone automaton: all its computations are j -monotone

Basic Correctness Preserving Property

- an $\text{hRLWW}(i)$ -automaton is **basically correctness preserving** if $u \Rightarrow_M^{C^*} v$ and $u \in L_C(M)$ induce that $v \in L_C(M)$, and therewith $h(v) \in L_{\text{hP}}(M)$ and $(h(v), v) \in L_A(M)$
- **Fact:** each deterministic $\text{hRLWW}(i)$ -automaton is basically correctness preserving.

Strong Cyclic Form

An **hRLWW**-automaton M is in **strong cyclic form** if it does not halt on any word of length greater than the size of its read/write window

Lemma 3

*Each **RLWW**(i)-automaton M can be transformed into **scf-RLWW**(i)-automaton M_{scf} such that*

- $L_C(M) = L_C(M_{\text{scf}})$,
- $u \Rightarrow_M^{C^*} v$ implies $u \Rightarrow_{M_{\text{scf}}}^{C^*} v$, for all words u, v ,
- *all reductions of M_{scf} that are not possible for M are in contextual form – they do not rewrite, delete at most two factors,*
- *if M is deterministic and/or j -monotone, then M_{scf} is deterministic and/or j -monotone.*

Strong Cyclic Form

Context-Free Constructions

- LRR = the class of left-to-right regular languages
- $\text{syn-RLWW}(i)$ means $j\text{-mon-RLWW}(i)$ where $j \leq i$

Theorem 4

Let $X \in \{\text{hRLWW}(1), \text{hRLWWD}(1), \text{hRLWWC}(1)\}$. Then

- $\text{LRR} = \mathcal{L}_C(\text{scf-det-syn-}X)$ and
- $\text{CFL} = \mathcal{L}_{\text{hP}}(\text{scf-det-syn-}X)$.

Sensitivity to the Size of Window

- Basic and h-proper languages of $\text{scf-hRLWW}(i)$ -automata are sensitive to the size of their windows, to the number of deletions by a reduction, and to the degree of monotonicity.
- small finite witness languages

Lemma 5

For $k \geq 2$:

- (a) $\{a^k\} \in \mathcal{L}_C(k\text{-scf-fin}(0)\text{-det-mon-RLWC})$.
- **RLWC-automata**: no auxiliary (non-input) symbols, contextual instructions only
 - **fin(0)**- at most 0 cycles in each accepting computation
 - k is the length of window
- (b) $\{a^k\} \notin \mathcal{L}_C((k-1)\text{-scf-hRLWW}) \cup \mathcal{L}_{\text{hP}}((k-1)\text{-scf-hRLWW})$.

Sensitivity to the Number of Rewrites per Cycle

- witness languages of cardinality two

Lemma 6

Let $k, j \geq 1$, let $L_2(j, k) = \{a^{k \cdot (j+1)}, a^k\}$.

- (a) $L_2(j, k) \in \mathcal{L}_C(k\text{-scf-fin}(1)\text{-det-mon-RLWC}(j))$.
- (b) $L_2(j, k) \notin \mathcal{L}_C(k\text{-scf-hRLWW}(j')) \cup \mathcal{L}_{\text{hP}}(k\text{-scf-hRLWW}(j'))$ for any $j' < j$.

Sensitivity to the Degree of Monotonicity

- finite witness languages

Lemma 7

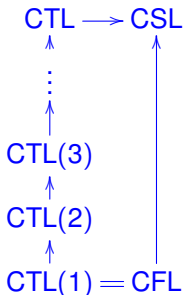
Let $k, j \geq 2$. There exist languages $L_3(j, k) \subset \{a, b, c\}^*$ of cardinality $j^2 + j + 1$ such that:

- (a) $L_3(j, k) \in \mathcal{L}_C(k\text{-scf-fin}(j + j^2)\text{-det-mon}(j)\text{-RLWC}(j))$.
- (b) $L_3(j, k) \notin \mathcal{L}_C(k\text{-scf-mon}(j')\text{-hRLWW}(j)) \cup \mathcal{L}_{\text{hP}}(k\text{-scf-mon}(j')\text{-hRLWW}(j))$ for any $j' < j$.
- (c) $L_3(j, k) \notin \mathcal{L}_C(k\text{-scf-hRLWW}(j')) \cup \mathcal{L}_{\text{hP}}(k\text{-scf-hRLWW}(j'))$ for any $j' < j$.

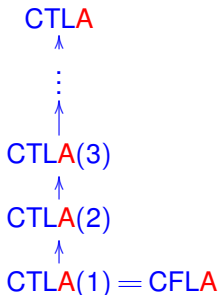
Hierarchy of Contextually Transparent Language Classes

$CTL(i)$ = the class of h-proper languages accepted by $hRLWW(i)$ -automata that are

- deterministic, contextual, in the strong cyclic form
- synchronized – $mon-(i)$



$CTLA(i)$ = the class of lexicalized analyses corresponding to $CTL(i)$



CTL \subsetneq CSL

\subseteq : easy

\subsetneq : $L_e = \{a^{2^n} \mid n \geq 0\} \notin \text{CTL}$ by contradiction

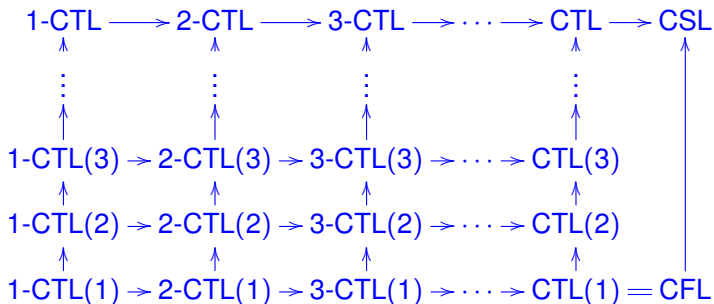
- if $a^{2^n} \in L_{\text{hp}}(M)$ for some k -hRLWW(i)-automaton, then $a^{2^n} = h(w)$ for some $w \in L_C(M)$ and there exists an accepting computation of M on w ; the accepting computation contains at least one cycle
- the cycle starts by a reduction $w \Rightarrow_M w'$, where $|w| > |w'| \geq |w| - k \cdot i$ and $h(w') \in L_{\text{hp}}(M)$
- for sufficiently large n , the length of $h(w')$ cannot be a power of 2 $\Rightarrow h(w') \notin L_{\text{hp}}(M)$ – a contradiction

A Refinement With Respect to the Window Size

h-Proper Language Classes

k -CTL(i) = the class of h-proper languages accepted by hRLWW(i)-automata that are

- deterministic, contextual, in the strong cyclic form
- synchronized – $\text{mon-}(i)$
- of window size k

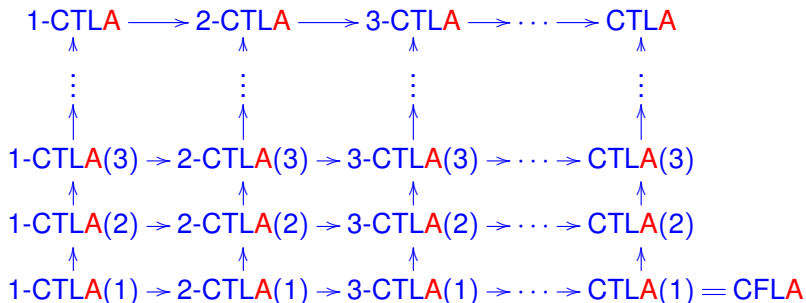


A Refinement With Respect to the Window Size

Lexicalized Analyses

k -CTLA(i) = the class of lexicalized analyses by hRLWW(i)-automata that are

- deterministic, contextual, in the strong cyclic form
- synchronized – mon- (i)
- of window size k



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- $\text{det-hRLWW}(i)$ -automata are **correctness preserving** with respect to their basic and h-proper languages, lexicalized syntactic analysis and analysis by reduction.

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- **Conjecture:** The lexicalized syntactic analysis of full (four level) FGD can be described by tools very close to $\text{24-CTLA}(4)$.

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- In traditional and corpus linguistics, only finite language phenomena can be directly observed. The basic and h-proper languages of $\text{hRLWWC}(i)$ -automata in strong cyclic form with constraints on the window size allow common classifications of finite phenomena as well as their infinite relaxations.
- Many practical problems in computational and corpus linguistic become decidable when we only consider languages parametrized by the size of the windows, or even easier when they are parametrized by a finite number of reductions.

Thank you for your attention!